# Age-of-Information With Information Source Diversity in an Energy Harvesting System

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Abstract—Age of information (AoI) is a key performance met-2 ric for the Internet of things (IoT). Timely status updates are 3 essential for many IoT applications; however, they often suffer 4 from harsh energy constraints and the unreliability of under-5 lying information sources. To overcome these unpredictabilities, 6 one can employ multiple sources that track the same process of 7 interest, but with different energy costs and reliabilities. We con-8 sider an energy-harvesting (EH) monitoring node equipped with 9 a finite-size battery and collecting status updates from multiple 10 heterogeneous information sources. We investigate the policies 11 that minimize the average AoI, formulating a Markov decision 12 process (MDP) to choose the optimal actions of either updating 13 from one of the sources or remaining idle, based on the current 14 energy level and the AoI at the monitoring node. We analyze 15 the structure of the optimal solution for different cost/AoI dis-16 tribution combinations, and compare its performance with an 17 aggressive policy that transmits whenever possible.

Index Terms—Age of information, energy harvesting, hetero geneous systems, Internet of Things, Markov decision process.

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AO1

AO2

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## I. INTRODUCTION

<sup>21</sup> **I** NTERNET OF THINGS (IoT) systems are increasingly <sup>22</sup> <sup>23</sup> being exploited for a variety of applications that encompass <sup>24</sup> every aspect of our lives [2]. In many of these applications <sup>24</sup> freshness of the monitored information can play an impor-<sup>25</sup> tant role for the system performance. Age of information <sup>26</sup> (AoI) is a key performance indicator in mission-critical and <sup>27</sup> time-sensitive applications, including smart transportation, <sup>28</sup> healthcare, remote surgery, robotics cooperation, public safety, <sup>29</sup> industrial process automation, to count a few. AoI quantifies <sup>20</sup> the freshness of knowledge about the status of the system <sup>31</sup> being monitored [3], [4]. For instance, in autonomous driving, <sup>32</sup> timely collection of traffic information and vehicle-generated

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data is essential for the safety of all road users. Another important example is factory automation, where real-time control of production also requires timely delivery of status updates [5]. 35

One limitation against frequent updates is the energy sup-36 ply of the sensor. Since sensing devices are typically wireless, 37 and often placed in remote areas, it would be impractical to 38 power them through cables. If the device is powered only through batteries, a significant downtime would hinder the 40 provision of reliable and up-to-date information. In these situa-41 tions, broad autonomy for reliable IoT systems can be obtained 42 through energy harvesting (EH) combined with rechargeable 43 batteries. This, however, would further require a smart sens-44 ing and communication strategy [6]. Indeed, the integration 45 of energy harvesters reduces the maintenance cost of IoT and 46 increases the energy self-sustainability, but comes at a price 47 of not guaranteeing uninterrupted operation of the device. 48

We focus on an EH monitoring node, whose goal is to 49 track the underlying process as closely as possible, i.e., with 50 the minimum average AoI, within the constraints of stochas-51 tic energy arrivals from ambient sources of energy and a 52 finite battery capacity. Also, we consider the role of multiple 53 information sources that monitor the same underlying pro-54 cess of interest called *information source diversity*, where each 55 source provides a different trade-off between the cost of sensing and the freshness of the provided status update. Hence, the 57 policy governing the operation of the system does not simply 58 make a binary choice between providing a new status update 59 or not, but must also include the optimal choice of the specific 60 information source to be used. To clarify, the policy might also 61 choose to wait, instead of updating immediately in a myopic 62 fashion, in order to accumulate energy so as to be able to use 63 a more reliable information source in the future. 64

We compare the performance of the optimal policy with 65 a greedy "aggressive" update policy in terms of average 66 AoI, highlighting the situations where optimization is really 67 needed as opposed to the simple implementation of an "update 68 whenever needed" strategy. We also quantify the additional gains in the minimal long-term average AoI due to multiple 70 information sources, as well as how the quality of these 71 sources affects the outcome. Finally, we compute the power 72 expenditure of these policies, and discuss how the added 73 dimensionality of the problem affects the system performance. 74

#### A. Background

Several papers study the average AoI minimization with <sup>76</sup> a single energy-harvesting source [7]–[19], whereas very <sup>77</sup>

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AQ4 Fig. 1. System model consisting of *n* information sources.

78 few papers are focused on the average AoI with multiple <sup>79</sup> information sources. In [20], [21], authors consider a system 80 where independent sources send status updates through a 81 shared first-come-first-serve M/M/1 queue to a monitor, and 82 find the region of feasible average status ages for two and <sup>83</sup> multiple sources. Similarly, in [22], a system with n sources <sup>84</sup> is considered to provide status updates to multiple servers via 85 a common queue. The authors formulate an AoI minimization <sup>86</sup> problem and propose online scheduling policies. In [23], a 87 single source node transmits status updates of two types to <sup>88</sup> multiple receivers. The authors determine the optimal stop-<sup>89</sup> ping thresholds to individually and jointly optimize the average 90 age of two-type updates at the receiver nodes. In [24], a <sup>91</sup> multi-objective formulation is proposed for scheduling trans-<sup>92</sup> missions in a system with multiple information sources that <sup>93</sup> monitor different processes. The objective is to balance the <sup>94</sup> AoI of these different processes. Similarly, in [25], the AoI 95 minimization problem is also formulated for a system with <sup>96</sup> multiple information sources that monitor different processes, <sup>97</sup> and a monitoring node that communicates with the information <sup>98</sup> sources through orthogonal channels. The authors propose the 99 policy that converts the scheduling problem into a bipartite 100 matching problem between the sets of channels and sensors. <sup>101</sup> In [26], the authors study the scenario where a base station <sup>102</sup> updates many network users. New information is randomly <sup>103</sup> generated, and the base station can serve at most one user for 104 each transmission. A structural MDP scheduling algorithm and an index scheduling algorithms were introduced. 105

One of the main challenges of deriving age-optimal trans-106 107 mission policies using MDP-based formulation is the large <sup>108</sup> size of the state space of the system. This problem has been <sup>109</sup> extensively studied for single-source systems. One of the ways 110 to tackle this challenge is by demonstrating the optimality 111 of a threshold-policy. In [27], the authors study a real-time 112 IoT-enabled monitoring system in which a source node is <sup>113</sup> responsible for maintaining the freshness of information status 114 at a destination node. The source node is powered by wire-115 less energy transfer. The authors adopt an MDP approach and <sup>116</sup> characterize the throughput-optimal policy. In [15], the authors 117 study the average AoI in EH cognitive radio communications, 118 where the secondary user, i.e., EH sensor, performs spectrum 119 sensing and status updates in a way that minimizes the aver-120 age AoI based on its energy availability and the availability 121 of the primary spectrum. The problem is formulated as a par-122 tially observable Markov decision process, and the optimal 123 sensing and updating policies are shown to have threshold 124 structure. The structural properties of the optimal policy for a single IoT device, where an IoT device updates the destination node via the wireless channel, are analysed in [28]. The authors consider a scenario where joint status sampling and updating process is designed to minimize the average AoI at the destination. The problem is formulated as an infinite horizon average cost constrained MDP that is transformed into an unconstrained MDP using a Lagrangian method. For the single IoT device, the optimal policy is shown to be of threshold type. Similar scenario is considered in [29], where an IoT device is classified as a secondary user that exploits the spectrum opportunities of the licensed band and updates the destination node.

Instead, the dimensionality problem in multi-source systems <sup>137</sup> is tackled in [30], where the authors consider a multi-source <sup>138</sup> RF-powered communication system and propose a reinforcement learning framework for optimizing the AoI. <sup>140</sup>

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#### B. Our Contributions

In this work, we consider a specific kind of multi-source 142 system, where the status updates are generated upon request by 143 an energy-harvesting monitoring node using multiple hetero- 144 geneous information sources that monitor the same underlying 145 process. These different sources may capture different phys- 146 ical phenomena from an abstract perspective. For example, 147 there may be multiple sensors monitoring the same process 148 of interest using distinct technologies for the transducers, thus 149 resulting in different accuracies and costs. Alternatively, the 150 heterogeneity of the sources may stem from different channels 151 that may convey the information (i.e., by means of different 152 technologies, routes, communication links, or all of the above). 153 Thus, each of the sources offers its own tradeoff of energy vs. 154 age, resulting in information source diversity, and the moni- 155 toring node may seek to optimize the resulting AoI over time. 156 This ought to take into account a constrained energy budget 157 and the characteristics of all the information sources. In our 158 model, each source may have available updates with different 159 ages, due to its sampling of the underlying process at possibly 160 diverse rates. 161

A sample scenario is crowdsensing, in which AoI can <sup>162</sup> play an important role when choosing the source of updates. <sup>163</sup> In crowdsensing, a monitor and some users are connected <sup>164</sup> via the cloud [31]. The monitor sends the sensing task <sup>165</sup> description to the users, and receives sensing plans, based on <sup>166</sup> which to perform user selection. The AoI received from each <sup>167</sup> information source depends on multiple factors such as sampling frequency, continuity of energy arrivals to the source <sup>169</sup> nodes (assuming that the source nodes are powered by the <sup>170</sup> ambient energy sources [32]), channel state, delay, and, in <sup>171</sup> general, the robustness of a node. <sup>172</sup>

Our first contribution is to analyze different heterogeneous <sup>173</sup> information sources, and study how the combinations of cost <sup>174</sup> and age distribution affect the resulting average AoI. We inves- <sup>175</sup> tigate the behavior of the optimal solution, which depends <sup>176</sup> on the configuration of the information sources, through <sup>177</sup> numerical analysis. In contrast to previous results in the lit- <sup>178</sup> erature [27]–[29], [33], we show through examples that the <sup>179</sup> optimal policy exhibits a threshold behavior only versus the <sup>180</sup> 181 AoI but in general not when the energy increases, since some182 times it may be convenient to refrain from updating and instead
183 cumulating energy for a later update from a more expensive
184 source.

As another contribution, we compare the performance of the optimal and aggressive policies, and find the threshold of the Hara EH rate in which it is reasonable to apply the aggressive policy. We evaluate the effect of an increase in the average system cost on the performance. Finally, we assess if an increase in the number of information sources affects the overall performance.

#### <sup>191</sup> C. Organization of the Paper

The rest of this paper is organized as follows. In Section II, 192 The system description, problem formulation, and solution 194 approaches are introduced. Numerical results are presented in 195 Section III, providing a comparison with an aggressive policy. 196 The paper is concluded in Section IV, where possible further 197 developments are also outlined.

### 198 II. SYSTEM MODEL AND PROBLEM FORMULATION

We focus on a communication system formed by a sin-199 gle energy-harvesting monitoring node and n heterogeneous 200 201 information sources, all capable of measuring the status of an underlying process. The monitoring node can query any 202 203 of these information sources to receive an update on the stas of the underlying process. For example, these information 204 205 sources may model sensors with different technologies mea-<sup>206</sup> suring the same process. In this paper, we consider such a general scenario, that could be further detailed to a multi-207 <sup>208</sup> sensor, multi-radio, or multi-transducer scenarios [34], [35]. <sup>209</sup> Time is divided into slots of equal length, and we assume that 210 the monitoring node can query from only one of the sources in each time slot. The received status update becomes available 211 212 at the beginning of the next time slot. We highlight two impor-213 tant dynamics at the monitoring node: 1) energy fluctuations <sup>214</sup> and 2) the AoI. The objective is to minimize the average AoI 215 at the monitoring node taking into account the time-varying 216 energy budget.

We assume that the monitoring node is equipped with a rechargeable battery of finite capacity *B*, and can harvest energy from ambient sources. Fluctuations in the battery of the monitoring node are defined by two processes: 1) harvested energy in each time slot and 2) the energy consumption caused by the queries for a status update. Energy harvested over time is represented as an independent and identically distributed (i.i.d.) binary random process  $\{e(t)\}_{t=1}^{\infty}$ . At each time slot *t* the monitoring node receives  $e(t) \in \{0, \overline{e}\}$  energy units, such that  $P(e(t) = \overline{e}) = \lambda$ .

The energy cost of requesting an update from source *i*,  $i \in [n] \triangleq \{1, 2, ..., n\}$ , is denoted by  $c_i$ , a collective value that reflects the energy consumption of the monitoring node to acquire an update from source *i*. This may include the cost of sending a request and receiving an update if the sources are remote sensors, or simply the cost of operating that sensor if they are local. For simplicity, we consider  $c_i \in \mathbb{Z}^+$ corresponding to integer multiples of a unit of energy. The AoI at time t, denoted by  $\delta(t)$ , refers to the age 235 of the most recent status update available at the monitoring node [36]. If a more recent update is not received, 237  $\delta(t)$  is increased by 1 at each time slot. We assume that 238  $\delta(t) \in [0, 1, \dots, \delta_{\max}]$ , as any AoI beyond  $\delta_{\max}$  has the same 239 utility for the system, which reduces the dimensionality of the 240 problem. 241

The status updates provided by the information sources are <sup>242</sup> not necessarily *fresh*, i.e., with zero age. Due to various factors, such as the sensing technology or the processing of the <sup>244</sup> measurements, we assume that the status updates may have <sup>245</sup> different ages when they arrive at the monitoring node. We <sup>246</sup> consider probabilistic AoI for the updates received from each <sup>247</sup> information source; that is, we assume that the source nodes <sup>248</sup> provide status updates with ages within the interval  $[\alpha, \beta]$  <sup>249</sup>  $(\alpha < \beta)$ , where  $\alpha$  is the most *fresh* status update while  $\beta$  is <sup>250</sup> the most *stale* one, typically with different distributions. We <sup>251</sup> assume that  $\alpha \ge 1$ , in order to incorporate the transmission <sup>252</sup> time of the status update. <sup>253</sup>

To model the different AoI distributions from each source, <sup>254</sup> denote by  $\gamma_{i,j}$  the probability of receiving a status update of <sup>255</sup> age *j* from source *i*, where  $j \in [\alpha, \beta]$  and  $i \in [n]$ . <sup>256</sup>

It is reasonable to assume that the sources with higher probability to deliver a fresh status update have a higher energy cost. Otherwise, a source which is both more costly and provides more stale state updates would never be used, and can safely be removed from the system model. 261

#### A. Markov Decision Process (MDP) Formulation

We aim to determine the policy that minimizes the average <sup>263</sup> AoI at the monitoring node. To achieve this, the monitoring <sup>264</sup> node optimally chooses the action to take at each time slot. <sup>265</sup> Possible actions include requesting an update from one of the <sup>266</sup> information sources at the beginning of each time slot, or staying idle. This choice is made taking into account the battery <sup>268</sup> level and the age of the most recent status update available at <sup>269</sup> the monitoring node. This problem can be formulated as an <sup>270</sup> MDP, consisting of a tuple <S, A, P, R>, where: <sup>271</sup>

- *S* is the state space where the process evolves;
- A is the set of actions to control the state dynamics; 273
- *P* denotes the state transition probability function;
- *R* is the reward function defined on state transitions. 275

The action taken by the monitoring node at time t is 276 denoted by a(t), chosen from a finite action space  $\mathcal{A} = 277$   $\{a_0, a_1, a_2, \ldots, a_n\}$ , where  $a_i$  corresponds to querying source 278 i for an update,  $i \in [n]$ , while  $a_0$  corresponds to remaining idle. 279 The system state is described by the pair of variables s(t) = 280  $(b(t), \delta(t)), \delta(t) \in [\delta_{\max}]$  and  $b(t) \in \lfloor B \rfloor \triangleq \{0, 1, \ldots, B\}$ . 281 We denote by  $\overline{\delta}(t)$  the age of the status update received at 282 time t. Note that  $\overline{\delta}(t)$  is a random variable depending on action 283 a(t). We set  $\overline{\delta}(t) = \delta_{\max}$  if  $a(t) = a_0$ . Moreover, if  $\overline{\delta}(t)$  happens to be larger than the age of the already available status 285 information,  $\delta(t-1) + 1$ , the current value is kept and no 286 update is performed. Thus, the AoI is updated as:

$$\delta(t) = \min\{\delta(t-1) + 1, \bar{\delta}(t), \delta_{\max}\}.$$
 (1) 28

The energy level in the battery b(t) at time *t* evolves according <sup>289</sup> to the cost of an action taken and the harvested energy within <sup>290</sup>

262

272

291 that time slot:

<sup>292</sup> 
$$b(t) = \min\left\{b(t-1) - \sum_{i=1}^{n} c_i \cdot \mathbb{1}(a(t) = a_i) + e(t), B\right\},$$
<sup>293</sup> (2)

where  $\mathbb{1}(x)$  is the indicator function:  $\mathbb{1}(x) = 1$  when x <sup>295</sup> holds, and  $\mathbb{1}(x) = 0$  otherwise. Action  $a_i$  is not allowed if 296  $b(t) < c_i, i \in [n]$ . We have a finite state space of dimension <sup>297</sup>  $\delta_{\max} \cdot (B+1).$ 

The transition probabilities are given below for  $a_i \in$  $\{a_1, a_2, \ldots, a_n\}$ , and  $\delta(t) \in \{\alpha, \alpha + 1, \ldots, \beta\}$ .

$$\begin{cases}
P[s(t+1) = (\min\{b + \bar{e} - c_i, B\}, \min\{j, \delta + 1, \delta_{\max}\}) \\
|s(t) = (b, \delta), a(t) = a_i] = \lambda \gamma_{i,j} \text{ for } b \ge c_i, j \in [\alpha, \beta], \\
P[s(t+1) = (b - c_i, \min\{j, \delta + 1, \delta_{\max}\}\}) \\
|s(t) = (b, \delta), a(t) = a_i] = (1 - \lambda) \gamma_{i,j} \\
\text{for } b \ge c_i, j \in [\alpha, \beta],
\end{cases}$$
(3)

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When the node stays idle, i.e.,  $a(t) = a_0$ , the transition 302 303 probabilities take the following form:

304 
$$P[s(t+1) = (b, \min\{\delta + 1, \delta_{\max}\})$$
  
305 
$$|s(t) = (b, \delta), a(t) = a_0] = 1 - \lambda \ b < B$$
  
306 
$$P[s(t+1) = (\min\{b + \bar{e}, B\}, \min\{\delta + 1, \delta_{\max}\})$$

$$\begin{array}{c} 300 \\ 307 \\ 1 \\ [b(t+1)] = (\min\{0+1, b\}, \min\{0+1, 0\max\}) \\ s(t) = (b, \delta), a(t) = a_0 \\ ] = \lambda \ b < B \end{array}$$

$$P[s(t+1) = (B, \min\{\delta+1, \delta_{\max}\})$$

$$s_{00} = [s(t) + 1) - (2, \min\{0 + 1, \max\})$$

$$|s(t) = (B, \delta), a(t) = a_0] = 1$$
(4)

310 Note that when the monitoring node chooses to stay idle and 311 its energy storage is full (i.e., B = b), the state transition only 312 involves the increase in the AoI since no more energy can be 313 stored in the battery, therefore this transition is deterministic.  $_{314}$  The reward received at time t depends on the action chosen 315 and the age of the update received at the monitoring node:

316 
$$R(s(t+1)|s(t), a(t) = a_i) = \delta(t+1).$$
 (5)

The problem is framed as a first-order Markovian dynamics 317 318 as the next state depends only on the current state s(t) and the 319 current action a(t).

The deterministic stationary policy  $\pi : S \to A$  defines an 320 action a(t) at each time slot depending on the current state. A set stationary policy  $\pi$  means that  $\pi_i = \pi$  for all  $t = 1, 2, \ldots, ;$ <sup>323</sup> we let  $\delta_t^{\pi}$  denote the sequence of AoI caused by policy  $\pi$ . The infinite-horizon time-average AoI, when policy  $\pi$  is employed, starting from initial state  $s_0$ , is defined as [36]:

<sup>326</sup> 
$$V^{\pi}(s_0) = \lim \sup_{T \to \infty} \frac{1}{T} \mathbb{E} \left[ \sum_{t=0}^T \delta^{\pi}(t) | s(0) = s_0 \right].$$
 (6)

A policy is *optimal* if it minimizes the infinite-horizon <sup>328</sup> average AoI -  $V^{\pi}(s)$ :

$$V(s) = \min V^{\pi}(s).$$
 (7)

330 To solve this optimization, we can use the offline dynamic <sup>331</sup> programming approach, which is a quite common methodol-332 ogy successfully used in other problems related to efficient 333 exploitation of harvested energy [37] and can be solved via

#### Algorithm 1 Relative VI Algorithm

set  $v^0(s) = 0 \ \forall s \in \mathcal{S}$ set  $n = 1, \epsilon > 0$ set  $V^0(s) = 0 \ \forall s \in \mathcal{S}$ repeat  $n \leftarrow n+1$ for all  $s \in \mathcal{S}$  do  $v^{n}(s) = \min_{a \in \mathcal{A}} \sum_{s' \in \mathcal{S}} P(s'|s, a) \Big[ \delta(s'|s, a) + V^{n-1}(s') \Big]$  $V^{n}(s) = v^{n}(s) - v^{n}(s_{0})$ where  $s_0$  is a fixed state chosen arbitrarily end for until  $sp(V^n - V^{n-1}) < \epsilon$ **return**  $\arg \min V(s)$ 

standard techniques such as Value Iteration [38]. In the offline 334 approach, we model the state transition function based on the 335 prior knowledge of the age statistics of the updates received 336 from different sources,  $\gamma_{i,j}$ , and the environmental character- 337 istics,  $\lambda$ . The solution represents the map of actions to be 338 chosen in different states. 339

#### **III. PERFORMANCE EVALUATION**

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We compare the effect of different cost combinations and 341 cost-reliability dependencies on the performance of differ- 342 ent policies. We consider the cost distribution of information 343 sources, the age distribution of updates received from different 344 sources, and the parameter of the EH process,  $\lambda$ . 345

To validate the optimal approach, we compare its 346 performance with that of the aggressive policy, which requests 347 a status update at each time slot from the most costly 348 information source that its current battery state affords. The 349 optimal solution is obtained via the value iteration (VI) algo- 350 rithm described in [38], which we also provide in Algorithm 1 351 for completeness. The optimal stationary deterministic policy 352 obtained by Algorithm 1 specifies the decision rules that maps 353 the current energy level and AoI to deterministic actions. 354

In Algorithm 1,  $sp(V^n - V^{n-1}) < \epsilon$  is a stopping criterion, 355 where  $sp(V) \triangleq \max_{s \in S} V(s) - \min_{s \in S} V(s)$ . We run the 356 relative VI algorithm until the stopping criterion holds. At 357 that moment the policy  $\pi$  achieves an average-cost AoI that is 358 within  $\epsilon \cdot 100\%$  of optimal. 359

#### A. Impact of Different Cost Functions

Since our model and formulation are fairly general, the 361 cost of requesting an update may result from very different 362 reasons (sampling, processing and/or communication costs). 363 Therefore, it is difficult to provide precise cost values and 364 their relation across sources. We assume that the energy cost 365 of any source takes values between  $c_{\min}$  and  $c_{\max}$ , where 366  $0 < c_{\min} < c_{\max} < B$ . In this way, we guarantee that all the  $_{367}$ sources are available to the monitoring node to query a status 368 update as long as there is sufficient energy in the battery. In 369 particular, we set the values of  $c_{\min} = 0.05B$ ,  $c_{\max} = 0.95B$ . 370

To evaluate the effect of different cost combinations of the 371 sources, we consider three cases, as per Fig. 2, each with the 372



Fig. 2. Rank-cost dependencies.



Fig. 3. Cost-age distribution dependency for the sublinear cost scenario.

<sup>373</sup> same average cost value: *superlinear*, *linear* and *sublinear*. In <sup>374</sup> Fig. 2, term 'Rank' corresponds to the index of source *i*, such <sup>375</sup> that a source with a higher index has a higher rank and higher <sup>376</sup> cost, respectively. The aforementioned dependencies do not <sup>377</sup> carry any special "physical meaning", they are simply chosen <sup>378</sup> to investigate the impact of cost values on the average AoI. <sup>379</sup> Indeed, other functions can also be used. Obviously, changing <sup>380</sup> the average cost will affect the average AoI, but the effect of <sup>381</sup> concavity on the target metric is not obvious. Thus, we focus <sup>382</sup> on these trends to analyse the effect of "concavity" on the <sup>383</sup> average AoI and also for easier reproducibility of our results.

#### 384 B. Impact of Different Cost-Reliability Dependencies

Further, we evaluate the impact of different functions describing the cost-reliability dependencies. Similar with the cost function, in order to be able to perform a comparison we limit our attention to a specific class of age distributions from the sources. In particular, in our numerical analysis we assume that, for each i,  $\gamma_{i,j}$  follows a geometric distribution with a different parameter  $p_i$ , as illustrated in Fig. 4. This model parameter. Hence, the distribution of the age of the received status update, when the *i*-th information source is chosen, is given by:

396 
$$\gamma_{i,j} = Pr(\bar{\delta}(t) = j) = (1 - p_i)^{j-1} p_i,$$
  
397  $j = 1, 2, 3, \dots, \beta - 1$ 

Since we consider that packets with age higher than  $\delta_{\max}$ have the same utility, we limit the geometric distribution to  $\delta_{\max}$ . Additionally,  $\gamma_{i,\beta} = Pr(\bar{\delta}(t) = \beta) = 1 - \sum_{j=1}^{\beta-1} (1 - p_i)^{j-1}p_i$  for every *i*. As stated earlier, we expect to receive more fresh status updates from a more costly source, at least on



Fig. 4. Geometric distribution of status updates for different  $p_i$  parameters, where  $\bar{\delta}(t) \in [1, 20]$ .

TABLE I Default System Parameters

Parameters	Values
Battery capacity, B	20
AoI values of received updates, $[\alpha, \beta]$	[1, 20]
Amount of harvested energy per time slot, $\{0, \overline{e}\}$	{0,3}
Number of sources, <i>n</i>	8
Cost range, $[c_{\min}, c_{\max}]$	[1, 19]
Maximum AoI, $\delta_{max}$	30

average. To quantify such a relation, we consider the following 403 general functional choices to relate  $p_i \in [0, 1]$  with  $c_i$  (Fig. 3): 404

Sublinear: 
$$p_i = k_{sub} \cdot c_i^2$$
, (9) 40

$$\text{Linear: } p_i = k_{lin} \cdot c_i, \tag{10} \quad 40$$

Superlinear: 
$$p_i = k_{sup} \cdot \log_2 c_i$$
, (11) 40

where  $k_{sub}$ ,  $k_{lin}$ , and  $k_{sup}$  are chosen such that the average 408 system parameters of age distribution  $(p = \gamma_i)$  is the same, i.e., 409  $\frac{1}{n} \sum_{i=1}^{n} p_i$  is equal for the sublinear, linear and superlinear 410 scenarios.

Once again, we would like to emphasize that our model and 412 solution tools apply to arbitrary cost and age distributions, and 413 these choices are made just to be able to observe the impact 414 of three possible dependencies on the performance. 415

#### C. Results

(8)

Default system parameters common to all the simula- <sup>417</sup> tions are presented in Table I. The efficiency of the optimal <sup>418</sup> and aggressive policies is verified via simulation runs over <sup>419</sup> T = 5000 time slots, averaged over M = 1000 simulations. <sup>420</sup> To demonstrate the results we plot the AoI averaged over all <sup>421</sup> times  $t = \overline{1, T}$ .

The optimal solutions for different values of EH rates 423 and cost-age distribution combinations are presented in 424 Figs. 5 and 6. Both figures show the 9 possible combina- 425 tions of cost and age distribution each taking values denoted 426 by superlinear, linear, sublinear as in (9)–(11), see also 427 Figs. 2 and 3. 428

We set  $\lambda = 0.2$  in Fig. 5 and  $\lambda = 0.6$  in Fig. 6. Each of <sup>429</sup> the 9 subfigures shows the optimal policy depending on the <sup>430</sup> system state. In both cases, n = 8 sources are considered, so <sup>431</sup> the optimal policy chooses among 9 possible actions including <sup>432</sup> "no update" (i.e., to stay idle). <sup>433</sup>



Fig. 5. Illustration of the optimal policy for different energy cost/ age distribution combinations for EH rate  $\lambda = 0.2$ .

Fig. 5 shows that when the EH rate is low, i.e.,  $\lambda = 0.2$ , 435 the monitoring node requests a status update only from the 436 cheapest sources, i.e., sources 1, 2. Notably, the result is sim-437 ilar for all the combinations of cost and age distributions. In 438 particular, the *activity region*, i.e., the set of states in which 439 the monitoring node is actively requesting updates, remains 440 the same. The activity region requires that both battery level 441 and AoI are high enough to request an update.

For low values of AoI, the monitoring node never requests a 442 443 status update, since the information is still fresh. Also, for low 444 values of the battery level a status update cannot be afforded. 445 However, differently from the aggressive approach, where an 446 update is always requested if there is enough energy in the 447 battery, the optimal policy, in contrast, conserves energy if 448 the AoI is sufficiently low. This leads to an energy saving 449 region for  $\delta(t) \in [0, \delta_u(b(t))]$ , where  $\delta_u(b(t))$  is the high-450 est AoI value for which no update is requested. The value 451 of  $\delta_u(b(t))$  decreases with b(t), because at high battery lev-452 els the monitoring node can be more relaxed in status update 453 requests. This trend applies for all cost-age distribution com-454 binations in the same way. The only difference appears when 455 the dependency of the parameters of the age distribution is 456 sublinear, due to the fact that the more expensive source 2 457 is significantly more reliable, and therefore, worth using at 458 higher energy levels. However, this also depends on the cost 459 of source 2; if the cost dependence is also sublinear then source 2 is employed instead of source 1 for lower values  $_{460}$  of b(t).

The common aspect of all the 9 subplots in Fig. 5 is that 462 only cheap sources are used when the energy arrivals are 463 scarce. In contrast, Fig. 6 shows more variations in the usage 464 of different sources for  $\lambda = 0.6$ . Here, similarly to Fig. 5, 465 the same 9 cases are considered in the respective subfigures. 466 For  $\lambda = 0.6$ , multiple sources are used depending not only 467 on the values of b(t) and  $\delta(t)$ , but also on the cost and age 468 distribution combinations. Even though the activity region is 469 approximately the same, it is split differently among multiple 470 sources, and not necessarily only the cheapest ones. In par- 471 ticular, the baseline case where cost and dependency of age 472 distribution parameters are both linear [Fig. 6(e)] demonstrates 473 that a wide array of sources from 1 to 5 (i.e., the 5 cheapest 474 ones) are used The higher b(t) and/or  $\delta(t)$ , the higher the index 475 of the source used for the update. 476

If we change the cost from superlinear to sublinear <sup>477</sup> [Figs. 6(b), 6(e), 6(h)], we see that, within the *activity region*, <sup>478</sup> source 1 is used more or less consistently in all the 3 cases, but <sup>479</sup> the patterns if other sources change, with intermediate sources <sup>480</sup> becoming more widely used if the cost is sublinear. This trend <sup>481</sup> is generally true if we read the subfigures from top to bottom. <sup>482</sup> Based on the structural difference of the optimal solutions, the <sup>483</sup> choice of the specific function is less important compared to <sup>484</sup> its characteristics in terms of concavity/convexity. <sup>485</sup>



Fig. 6. Illustration of the optimal policy for different energy cost/ age distribution combinations for EH rate  $\lambda = 0.6$ .

Conversely, if we change the dependency of age distribu-487 tion parameters [Figs, 6(d), 6(e), 6(f))], the cheaper sources 488 are used more often, and their usage happens at lower bat-489 tery levels, i.e., their region shifts towards left. This trend 490 is also generally true if we read the subfigures from left 491 to right.

#### 492 D. Discussion

In this section, we prove some structural property of the 494 optimal policy, in particular, an existence of a threshold effect 495 on the battery level *b* (but notably, not on  $\delta$ ).

Theorem 1: If the AoI is unlimited (or, its maximum  $^{496}$  value is sufficiently high) then the optimal policy has an  $^{498}$  AoI-threshold-based behavior that holds for any value of *b*.

This means that if we focus on a given *b*, the optimal policy depends on the AoI  $\delta$  such that:

• a given subset of k(b) sources is used, denoted by  $\sigma_1(b), \sigma_2(b), \dots \sigma_{k(b)}(b) \in [N],$ 

• exactly k(b) threshold values for the AoI  $\delta$ , denoted by  $\vartheta_1(b), \vartheta_2(b), \dots, \vartheta_{k(b)}(b)$  can be defined, in strictly increasing order (i.e.,  $\vartheta_j(b) < \vartheta_{j+1}(b)$  for every  $j \in [N-1]$ ), so that source  $\sigma_j(b)$  is used only when  $\vartheta_j(b) \leq \delta < \vartheta_{j+1}(b)$  for  $j \in [N-1]$ , and the last source  $\sigma_{k(b)}$ is used for  $\delta \geq \vartheta_{k(b)}(b)$ , while no update is attempted if  $\delta < \vartheta_1(b)$ .

This threshold-based character of the optimal policy under the aforementioned conditions, can be proven through the file following two lemmas. *Lemma 1:* A system with  $n \ge 2$  sources has an optimal 513 AoI-threshold-based activation  $\vartheta_1(b)$  for all values of e, mean-514 ing the optimal policy is to stay idle (action  $a_0$ ) when  $\delta < 515$  $\vartheta_1(b)$ , and conversely action  $a_0$  is suboptimal if  $\delta \ge \vartheta_1(b)$ . 516 *Proof:* The details are reported in Appendix A.

Following this Lemma, one can see that if  $\delta \geq \vartheta_1(b)$  518 it is convenient to update but it is not knowns from which 519 source. We need to obtain a full AoI-threshold-based structure 520 as required by the theorem to show that, if a given *b* is con-521 sidered and  $\delta$  is increased from  $\vartheta_1(b)$ , there are other turning 522 points  $\vartheta_2(b), \vartheta_3(b), \ldots$  such that for  $\delta \geq \vartheta_j(b)$  the optimal 523 action switches from  $s_j(b)$  to  $s_{j+1}(b)$  and *never reverts back* 524 to  $s_j(b)$  after that point. This is shown through this last 525 Lemma. 526

*Lemma 2:* Consider a given value of *b* and two different <sup>527</sup> sources *i* and *j*, whose associated update actions are  $a_i$  and <sup>528</sup>  $a_j$ , respectively. If  $a_i$  is preferable over  $a_j$  when the battery <sup>529</sup> level is *b* and the AoI value is  $\delta_1$ , where  $\delta_1 \ge v_1(b)$ , and the <sup>530</sup> reverse happens (i.e.,  $a_j$  is preferable over  $a_i$ ) for battery level <sup>531</sup> *b* and AoI equal to  $\delta_2 > \delta_1$ , then  $a_j$  is necessarily better than <sup>532</sup>  $a_i$  for battery level *b* and all AoI values  $\delta > \delta_2$ .

The proof is provided in Appendix B. We remark that  ${}^{534}$  the theorem proves an AoI-threshold-based behavior, but in  ${}^{535}$  general we do not have a similar behavior in the battery level  ${}^{536}$  b, as discussed in the following counterexample.  ${}^{537}$ 

*Counterexample:* Consider a scenario with two information 538 sources, where  $\delta_{\text{max}} = 1$ , and  $\alpha = 0$   $\beta = 1$ . The two 539



Fig. 7. Optimal solution  $(p_2 = 1, p_1 = 0.1, \lambda = 0.9)$ .



Fig. 8. Optimal solution: N = 1,  $p_2 = 0.99$ ,  $c_1 = 5$ ,  $c_2 = 11$ ,  $\lambda = 0.9$ ,  $\bar{e} = 5$ .

<sup>540</sup> information sources 1 and 2 have the following characteristics: <sup>541</sup>  $0 < c_1 < c_2 < B$ ,  $p_2 \gg p_1$ .

<sup>542</sup> Compare the time-average AoI for T = 2 for the following <sup>543</sup> sequences of actions performed by the monitoring node:

Sequence 1: (use 1; use 1), resulting in  $\overline{\delta} = 1 - p_1 + \frac{(1-p_1)^2}{2}$ . Sequence 2: (do not transmit; use 2), resulting in  $\overline{\delta} = 1 + \frac{1-p_2}{2}$ .

<sup>547</sup> If  $p_2 > 4p_1 - p_1^2$ , then sequence 2 is preferrable over <sup>548</sup> sequence 1. However, sequence 2 may not be available if <sup>549</sup> using source 2 is too expensive for the current battery state. In <sup>550</sup> other words, depending on the current energy state and energy <sup>551</sup> arrivals, it may be more convenient to just use the cheap source <sup>552</sup> or to wait in order to enable the expensive source in the subse-<sup>553</sup> quent time slot. Formally, this happens if  $b(0) - c_1 + \lambda h > c_2$ . <sup>554</sup> Hence, we proved that with an increase in the state of the bat-<sup>555</sup> tery at time 0, the minimization of AoI can imply to use a <sup>556</sup> *cheaper* source at time 1 (in this specific example, no source <sup>557</sup> at all), which contradicts the monotonicity of the source index <sup>558</sup> in the battery level.

In Fig. 8, we demonstrate the effect of limiting N on the structure of the optimal solution. We considered a system with two sources with  $p_1 = 0.2$ ,  $p_2 = 0.99$ ,  $c_1 = 5$ ,  $c_2 = 11$ . The AoI distribution is kept geometric in range  $[\alpha, \beta] = [0, 20]$ . The energy-harvesting process is given with parameters  $\lambda = 0.9$ ,  $\bar{e} = 5$ . We observe the energy saving region that occurs under this particular combination of parameters.

Another visual counterexample is also graphically presented form Fig. 7, where we adopt the default settings from Table I, and consider two sources such that  $p_2 \gg p_1$ ,  $\lambda = 0.9$ . We for also increased the value of parameter  $\bar{e}$  so that the energy buffer can recover fast. The costs of sources are set as follows for also increased the value of parameter  $\bar{e}$  so that the energy form buffer can recover fast. The costs of sources are set as follows for  $c_1 = 1, c_2 = 16$ . The distribution of AoI is preserved as geometric in range  $[\alpha, \beta] = [1, 20]$ . In this setup, the optimal policy is not threshold-based with respect to the battery level.



Fig. 9. Rate between the average AoI obtained by the optimal and aggressive policies as a function of the EH rate.



Fig. 10. EH rate,  $\lambda$  vs average AoI and average energy consumption.

#### E. Performance Comparison

To understand the potential benefits of the optimal policy, 576 we compare it with the aggressive policy as a benchmark. 577 In Fig. 9 we plot the relative gain over the aggressive pol- 578 icy vs the EH rate  $\lambda$ , where the AoI-aggressive-efficiency in 579 the y-axis is defined as the ratio between the average AoI 580 obtained by the optimal strategy to the one obtained by the 581 aggressive policy. For the sake of brevity, five cost and age 582 distribution combinations are considered. High (close to 1) 583 AoI-aggressive-efficiency implies that the aggressive policy is 584 quite efficient, and benefit of using the more computationally 585 demanding VI framework is limited. Despite some differ- 586 ences in the structure of the optimal solution, the resulting 587 AoI-aggressive-efficiency has similar values for all cost-age 588 distribution combinations. The AoI-efficiency-rate increases 589 with  $\lambda$ , meaning that the difference in performance between 590 optimal and aggressive policy vanishes at high  $\lambda$ . In particu- 591 lar, for  $\lambda > 0.5$  the AoI-aggressive-efficiency saturates above 592 0.90. We can conclude, that if the energy arrivals are rela- 593 tively stable, the benefits of optimization is rather limited. On 594 the other hand, for low values of  $\lambda$  the optimization of the 595 update policy is much more relevant, which follows the intu- 596 ition. Yet, when  $\lambda$  is very low, the role of multiple sources is 597 minimal, and only the cheapest sources are used (see Fig. 5). 598

In Fig. 10, we plot the average AoI and the average energy 599 consumption vs. the EH rate. As one would expect, the average 600 energy consumption increases with  $\lambda$ , while the average AoI 601 decreases. We observe that the two policies have almost identical energy consumption, for low  $\lambda$  values, although the optimal 603 policy provides significantly lower average AoI performance. 604



Fig. 11. EH rate,  $\lambda$ , vs average AoI for linear cost-age distribution.

<sup>605</sup> Also, the energy consumption of the aggressive policy satu-<sup>606</sup> rates at high  $\lambda$  values, while that of the optimal policy continue <sup>607</sup> to increase linearly.

We also analyzed the average AoI when the average update for cost is 50% higher than the default case. To do so, we for increased the cost of each source 1.5 times (1.5*C*) and found for the linear cost-age distribution case, as for demonstrated in Fig. 11. With the increase of cost, the differfor ence between the average AoI achieved by the optimal and for aggressive policies reaches up to 15%, if  $\lambda$  is low. When  $\lambda$  is for high, the difference in performance is insignificant.

#### 616 F. Network Size

Further, we analyze how the number n of information 617 618 sources affects the performance for different values of EH 619 rate,  $\lambda$ , and energy arrival units,  $\bar{e}$ . The analysis is performed 620 for linear scaling of the costs of the devices, and a linear 621 dependency between the cost and the number of the sources. We decrease the space of actions (or network size) in the 622 623 following manner: first, we form the vector of size *n* with costs  $[c_1, c_2, \ldots, c_n]$ , and derive the average AoI for *n* information 624 sources. Then, we reduce the network size by half at each step 625 till we have only two information sources with cost vector 626  $[c_1, c_n]$ , thus we obtain the average AoI for n = 2, 4, 8, 16. 627 <sup>628</sup> For n = 12, we randomly removed four sources.

Firstly, we consider a system without sources diversity, i.e., 629 630 with a single information source; and demonstrate the depen-631 dency of optimal average AoI and cost of that source. With 632 the increase in the cost, the optimal average AoI increases, 633 despite the fact that with the increase of the cost, the proba-634 bility to receive a fresh status update increases. Moreover, in 635 the greatest extent, an increase in cost affects the performance 636 in case of low frequency energy arrivals (see Fig. 12). If the  $c_{037}$  cost value is low, i.e.,  $c_1 = 1$ , the performance for different values of  $\lambda$  has minor variation. In particular, the performance 638 identical if  $\lambda$  is sufficiently high ( $\lambda > 0.4$ ). Although, when 639 is = 0.2 the optimal solution has a larger energy saving area, λ 640 which is why we observe a larger gap in performance. 641

With the increase in the number of information sources, the optimal average AoI has a tendency to decrease, but the curves eventually saturate when the number of sources reaches n = 8(Fig. 13). The largest gain in performance is obtained when eventually solve n = 2. If the EH rate is low ( $\lambda = 0.2$ 



Fig. 12. Optimal average AoI vs. cost of an information source for different values EH rates,  $\lambda$ .



Fig. 13. Optimal average AoI vs. number of information sources for different values of EH rates,  $\lambda$ .

in Fig. 13), then the increase in the number of devices does <sup>647</sup> not provide any gain for the system performance, but with <sup>648</sup> an increase in the EH rate, the gain increases as the system <sup>649</sup> size goes from n = 1 to n = 2 if  $\lambda \leq 0.6$ . If  $\lambda \geq 0.4$  the <sup>650</sup> gain obtained by an increase of the system size from n = 1 <sup>651</sup> to n = 2 and from n = 2 to n = 4 is similar. Nevertheless, <sup>652</sup> in the performance comparison in case of n = 1 we consider <sup>653</sup> the best performing setting, i.e.,  $c_1 = 1$ ,  $p_1 = 0.1$ . If  $c_1 > 1$ , <sup>654</sup>  $p_1 > 0.1$ , the gain is much more significant when the system <sup>655</sup> size is increased from n = 1 to n = 2. A similar statement <sup>656</sup> holds true when we vary the values of energy arrivals,  $\bar{e}$ . This <sup>657</sup> is because, when the EH rate is low, the monitoring node <sup>658</sup> almost exclusively uses the "cheaper" information sources, so <sup>659</sup> introducing more expensive alternatives does not help.

If the monitoring node exploits the aggressive strategy, then <sup>661</sup> we observe a counterintuitive behaviour: with an increase <sup>662</sup> in the system size for n > 2, the performance worsens, <sup>663</sup> or, in other words, the average AoI at the monitoring node <sup>664</sup> increases. Moreover, the lower  $\lambda$ , the higher the increase <sup>665</sup> in the average AoI, or the more inefficient the aggressive <sup>666</sup> policy becomes. This effect is particularly negative for low <sup>667</sup>  $\lambda$  values because the aggressive policy always goes for the <sup>668</sup> most expensive information source it can afford. Introducing <sup>669</sup> more expensive alternatives means that they will end up being <sup>670</sup> used rather than the cheaper sources. This results in a poorer <sup>671</sup> performance particularly for low  $\lambda$  values, when it is optimal <sup>672</sup> to exploit only the cheapest sources. Yet, when  $\lambda \ge 0.4$  introducing system diversity slightly improves the performance; <sup>674</sup>



Fig. 14. Average AoI vs. number of information sources vs. if the monitoring node adopts aggressive strategy for different values of the EH rate,  $\lambda$ .

<sup>675</sup> actually, the best performance is provided by  $c_1 = 8$  (see <sup>676</sup> Fig. 12), therefore, when we shift from C = [1] to C = [16, 1]<sup>677</sup> we achieve the "balance" and an improvement in the <sup>678</sup> performance. However, with a further increase of the system <sup>679</sup> size the "balance" shifts causing an increase in average AoI <sup>660</sup> (see Fig. 14).

#### IV. CONCLUSION

In this work, we considered a system model with a single energy-harvesting monitoring node that can request status updates from multiple heterogeneous information sources that monitor the same process of interest. We assumed that the energy cost of requesting an update, as well as the statistics of the age of the received update varies across the information sources. In order to analyze the system, we considered different combinations of costs and age distributions that are described in detail in Section III.

We formulated the long-term average AoI minimization problem as an MDP, and obtained the optimal solution using the relative VI algorithm. We then studied the optimal solution for different EH rates and found out that the solutions are more sensitive to the age distribution rather than the costs of the status updates. We demonstrated that having rate is low. We also considered an aggressive policy, which requests a status update from the most expensive source it roo can afford at each time slot, as a benchmark. We observed rot that the aggressive policy is near optimal when the EH rate roz is high.

We found that adding information sources beyond a certain number does not help, particularly if the available sources already provide sufficient diversity in terms of the cost-average age trade-off within the available energy sources.

Future work includes an extended model comprising the channel dynamics and the resulting transmission time and costs, as well as more general EH schemes [39]. Another direction is to study reinforcement learning to choose the r11 information source to use over time without depending on the r12 explicit information on the age distributions of the sources or r13 the statistics of the EH process [30].

#### APPENDIX A 714 PROOF OF LEMMA 1 715

The lemma requires to prove, for any *b*, the existence of a 716  $\vartheta_1(b)$  such that it is convenient to update if and only if  $\delta \ge 717$   $\vartheta_1(b)$ . First of all, for  $b < b_0 = \min_{j=1,2,...,N} c_j$ , then the 718 statement is trivially true with an infinite  $\vartheta_1(b)$  as all sources 719 are too expensive to update.

Define  $\overline{R}(s(t) = (b, \delta), a_i)$  as the average optimal reward <sup>721</sup> starting from the current state  $s(t) = (b, \delta)$  and after taking <sup>722</sup> action  $a(t) = a_i$ . According to our model, if i > 0, that is, <sup>723</sup> we perform an actual update from source i, we evolve to a <sup>724</sup> state with either energy level  $b - c_i$  or  $b - c_i + \overline{e}$  (depending <sup>725</sup> on the EH process) and AoI  $\epsilon \in \mathcal{E}_i = [\alpha, \min(\beta, \delta + 1)]$  with <sup>726</sup> probability  $\tilde{\gamma}_i(\epsilon)$ , which is defined as follows. If  $\beta \leq \delta$  then <sup>727</sup>  $\tilde{\gamma}_i(\epsilon) = \gamma_i(\epsilon)$  for all  $\epsilon$ . If  $\beta > \delta$  then  $\tilde{\gamma}_i(\epsilon) = \gamma_i(\epsilon)$  for  $\epsilon \in [\alpha, \delta]$  <sup>728</sup> and  $\tilde{\gamma}_i(\delta + 1) = \sum_{n=\delta+1}^{\beta} \gamma_i(n)$ . <sup>729</sup> From (4) and (5) we can write the following Bellman <sup>730</sup>

From (4) and (5) we can write the following Bellman  $_{730}$  equation for  $\bar{R}(s(t), a_i)$  being  $_{731}$ 

Г

$$\max_{j\in\Omega} \left[ (1-\lambda) \sum_{\epsilon\in\mathcal{E}_i} \left( \epsilon + \tilde{\gamma}_i(\epsilon) \bar{R} \left( s(t+1) = (b-c_i,\epsilon), a_j \right) \right) \right]$$
 732

$$+ \lambda \sum_{\epsilon \in \mathcal{E}_i} \left( \epsilon + \tilde{\gamma}_i(\epsilon) \bar{R} \left( s(t+1) = (b - c_i + \bar{e}, \epsilon), a_j \right) \right), \quad \text{733}$$

where 
$$\Omega = \{0, ..., n\}$$
 (12) 734

Given that  $\epsilon$  does not depend on  $a_i$ , (12) can be written as: 735

$$(1-\lambda)\sum_{\epsilon\in\mathcal{E}_i} \left(\epsilon + \tilde{\gamma}_i(\epsilon)\max_{j\in\Omega}\bar{R}\left(s(t+1) = (b-c_i,\epsilon), a_j\right)\right) \quad \text{736}$$

$$+ \lambda \sum_{\epsilon \in \mathcal{E}_i} \left( \epsilon + \tilde{\gamma}_i(\epsilon) \max_{j \in \Omega} \bar{R} \left( s(t+1) = (b - c_i + \bar{e}, \epsilon), a_j \right) \right)$$
 737

(13) 738

739

whereas if we do not update (action  $a_0$ ) we obtain

$$\bar{R}(s(t), a_0) = (1 - \lambda)$$
740

$$\times \left(\delta + \max_{j \in \Omega} \bar{R}(s(t+1) = (b, \delta+1), a_j)\right)$$
741

$$+\lambda \left(\delta + \max_{j\in\Omega} \bar{R}\left(s(t+1) = (b+\bar{e},\delta+1), a_j\right)\right)$$
(14) 742
(14) 743

We notice that (13) is not explicitly influenced by  $\delta$ , which 744 is incidentally logical as, after the update,  $\delta$  is reset to a "low" 745 AoI value, <sup>1</sup> whereas (14) is increasing in  $\delta$ . This implies that as 746  $\delta$  increases, there exists a turning point  $\vartheta_1(b)$  that makes (13) 747 smaller than (14) and this stays true for all values of  $\delta \geq$  748  $\vartheta_1(b)$ . 749

Similarly to the previous lemma, we can compare the 752 Bellman equations for the updates from two different sources 753

<sup>&</sup>lt;sup>1</sup>To be precise, the set  $\mathcal{E}_i$  actually depends on  $\delta$  but only for the reason that whenever the update is supposed to be to a value in  $[\alpha, \beta]$  that is higher than  $\delta + 1$ , the update information is actually useless and discarded, see (1).

<sup>754</sup> *i* and *j*. Note that we are always considering AoI values <sup>755</sup>  $\delta > \vartheta_1(b)$  for which an update is preferable to staying idle, as <sup>756</sup> proven in Lemma 1. And since we are updating in both cases, <sup>757</sup> we lose any explicit dependence on the AoI  $\delta$ , as per (13) -<sup>758</sup> in other words, after either update action, the system trajec-<sup>759</sup> tory evolves from states with "low" AoI. Finally, we remark <sup>760</sup> that  $\bar{R}((b,\delta), a)$  is always non-decreasing in  $\delta$  for given *b* and <sup>761</sup> action *a*. This implies that if  $\bar{R}((b,\delta_1), a_i) < \bar{R}((b,\delta_1), a_j)$ <sup>762</sup> but  $\bar{R}((b,\delta_2), a_i) > \bar{R}((b,\delta_2), a_j)$ , then  $\bar{R}((b,\delta), a_i) >$ <sup>763</sup>  $\bar{R}((b,\delta), a_j)$  also for every  $\delta > \delta_2$ ; that is, a source to update <sup>764</sup> from can be the optimal one only over a set of contiguous AoI <sup>765</sup> values.

#### 766

AO5

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