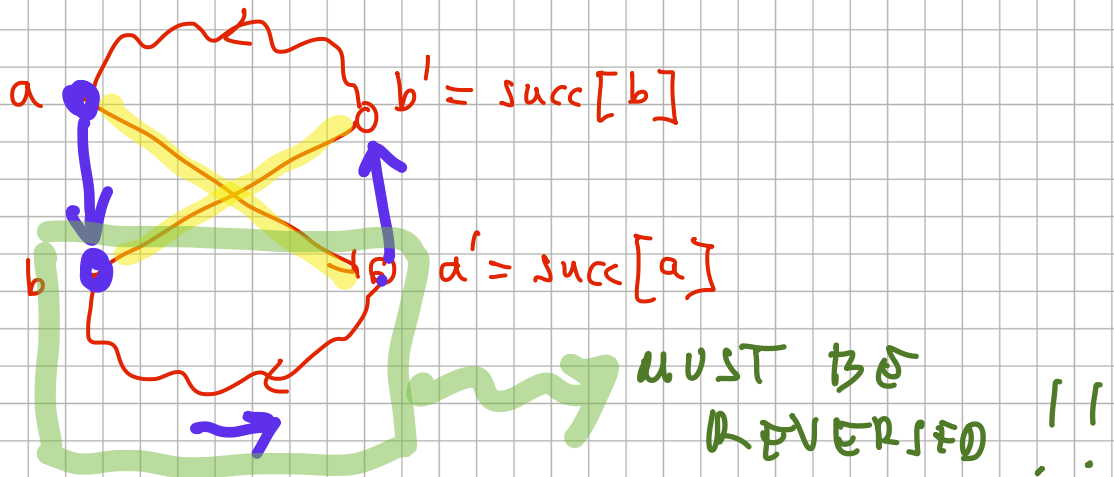


REFINEMENT ALG.

2-OPT MOVE



$$\Delta \text{cost}(a,b) = \text{new-old cost} = \underbrace{(c[a,b] + c[a',b'])}_{\text{new cost}} - \underbrace{(c[a,a'] + c[b,b'])}_{\text{old cost}}$$

$< 0 \Rightarrow$ improve current sol. by implementing the 2-opt move



\rightarrow TRY all (a,b) pairs \rightarrow

$\Delta \text{cost}(a^*,b^*)$ is a minimum

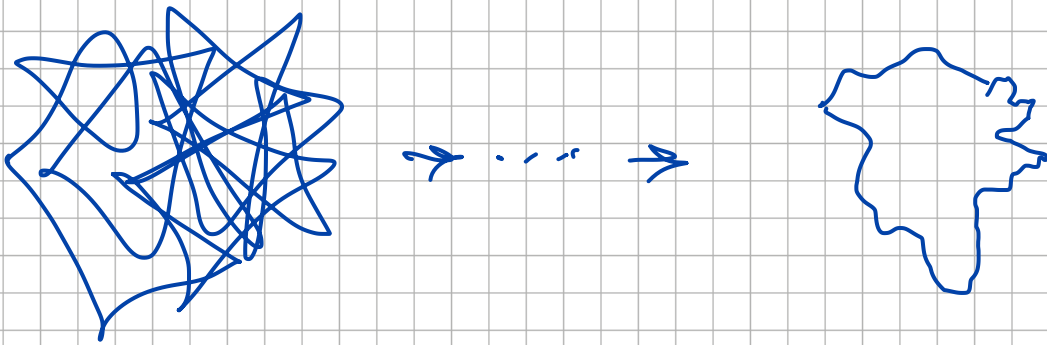
$\Delta \text{cost}(a^*,b^*) < 0 \Rightarrow$ implement & repeat

$$\frac{n \cdot (n-1)}{2}$$

options

$$\approx O(n^2)$$

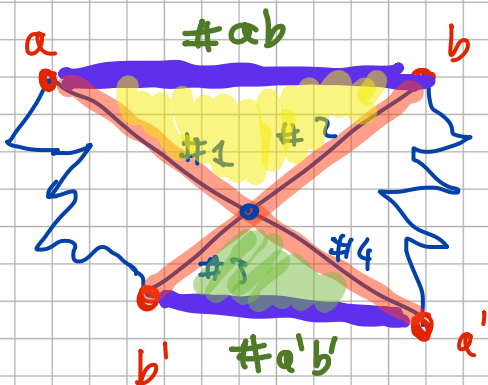
$\Delta \text{cost}(a, b)$ takes $O(1)$ time
(constant)



RANDOM MULTI-START + (2-OPT)

(GREEDY + GRASP) → 2-OPT

(EXTRA-MILEAGE + GRASP) → 2-OPT



EUCLIDEAN-DISTANCES

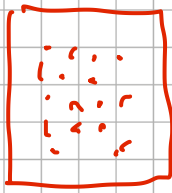
$$\Delta \text{cost}(a, b) < 0$$



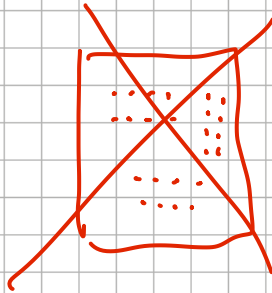
HOW TO COMPARE ~~OPT.~~ ALG.S ?

HEUR.

- FIX A TIME-LIMIT (5-MINUTES ?)
 - TEST BED " training / validation set in ML "
- ~ 100 instances



random
in the
1000x1000
square



• COMPARISON AMONG HEURISTICS

~~TIME LIMIT~~
FIXED

QUALITY OF THE
SOL \rightarrow COST

" the lower the
better "

EX

3 competing ALG.S

— 1 — 2 — 3

NAIVE COMPARISON: AVERAGE COST \rightarrow MINIMUM!

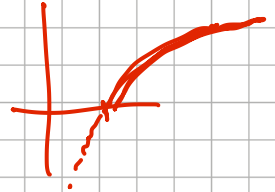
GEO. MEAN COST \rightarrow MINIMUM!

$$\frac{\sum_{k=1}^n v_k}{n}$$

AR. MEAN (AVERAGE)

$$\left(\prod_{k=1}^n v_k \right)^{1/n}$$

GEO. MEAN

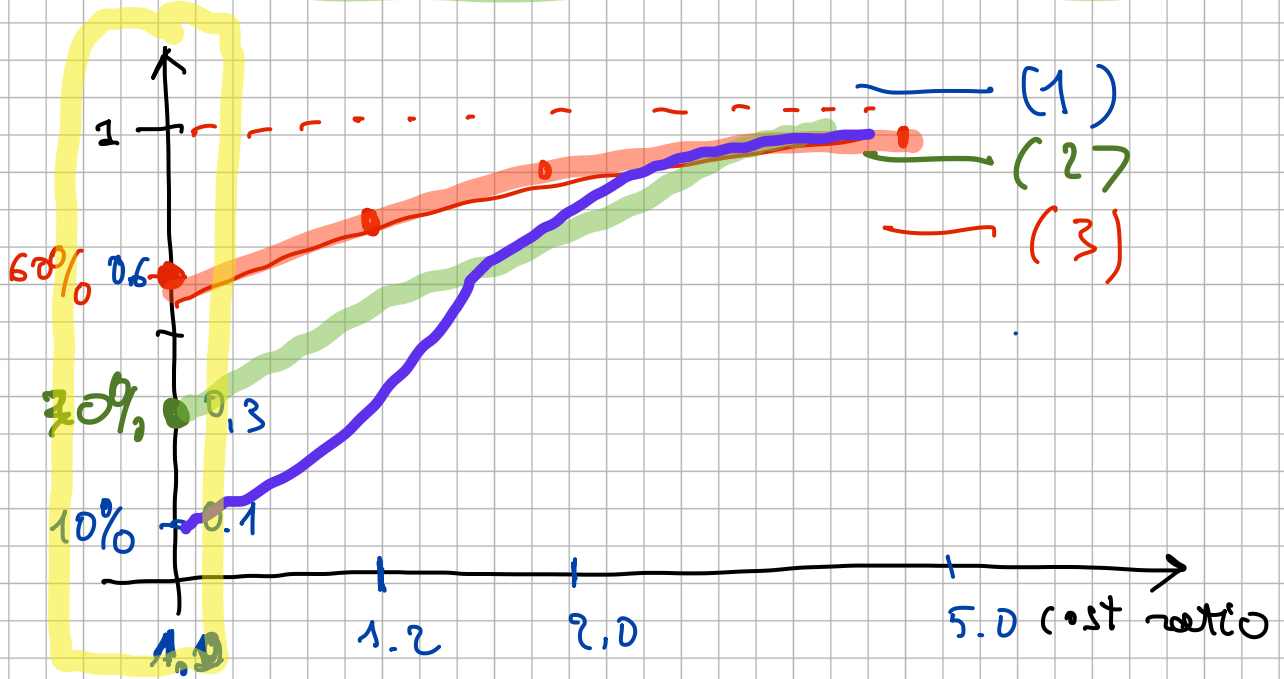


$$\log \left(\prod_{k=1}^n v_k \right)^{1/n} = \frac{1}{n} \sum_{k=1}^n \log(v_k)$$

average of the log \rightarrow

STATE-OF-THE-ART

PERFORMANCE PROFILE PLOTS



NAME	ALG. 1	ALG. 2	ALG. 3
seed 1	123.5	175.7	101.7
... 2	377.2	371.9	377.2
...			
seed 100	105.7		

↑ cost

NAME	ALG. 1	ALG. 2	ALG. 3
seed 1	1.2	1.7	1.0
... 2			1.0
...		1.0	1.0
...	1.0		1.0
...	1.0		1.0
seed 100	105.7		

↑ RATIOS WRT
BEST

